

# Measurement of Environmental Parameter (i.e. Strain) by using Bragg Grating Sensor for Structural Health Monitoring Application

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**Abstract-** Here in this paper we presented the modelling of FBG as Strain sensor for structural health monitoring application is geometrically designed in the wavelength window of 1.568-1.580µm. Simulation has been done by using optical software R-Soft (GratingMOD).

**Keywords-** FBG, SHM, GratingMOD, Strain.

## 1. Introduction

Modelling and simulation are mathematical models that allow representing the dynamics of the system via simulation, allows exploring system behaviour in an articulated way which is often either not possible, or too risky in the real time. Fibre Bragg grating (FBG) sensors have been investigated intensively in the past few years due to its small size and robustness, ease of fabrication, suitability for use in multiplexed sensor networks and smart structures [2]. In this paper we represent the modelling of FBG for strain sensor for structure health monitoring.

## 2. Fiber Bragg Grating

Consider a uniform Bragg grating formed within the core of an optical fibre with an average refractive index  $n_0$ . The index of the refractive profile can be expressed as

$$n(z) = n_0 + \Delta n \cos\left(\frac{2\pi z}{\Lambda}\right) \dots (1)$$

Where  $\Delta n$  is the amplitude of the induced refractive index perturbation (typically  $10^{-5}$  to  $10^{-2}$ ) and  $z$  is the distance along the fibre longitudinal axis. Using coupled-mode theory [1] the reflectivity of a grating with constant

modulation amplitude and period is given by the following expression

$$R(l, \lambda) = \frac{k^2 \sinh^2(sl)}{\Delta\beta^2 \sinh^2(sl) + s^2 \cosh^2(sl)} \dots (2)$$

where  $R(l, \lambda)$  is the reflectivity, which is a function of the grating length  $l$  and wavelength  $\lambda$ .  $k$  is the coupling coefficient,  $\Delta\beta = \beta - \pi/\Lambda$  is the detuning wave vector,  $\beta = 2\pi n_0/\lambda$  is the propagation constant and finally  $s^2 = k^2 - \Delta\beta^2$ . For sinusoidal variations of the index perturbation the coupling coefficient,  $k$ , is given by

$$k = \frac{\pi \Delta n}{\lambda} M_{power} \dots (3)$$

Where  $M_{power}$  is the fraction of the fibre mode power contained by the fibre core. In the case where the grating is uniformly written through the core,  $M_{power}$  can be approximated by  $1 - V^{-2}$ , where  $V$  is the normalized frequency of the fibre, given by

$$V = (2\pi/\lambda) a \sqrt{n_{co}^2 - n_{cl}^2} \dots (4)$$

Where  $a$  is the core radius, and  $n_{co}$  and  $n_{cl}$  are the core and cladding indices, respectively. At the centre wavelength of the Bragg grating the vector detuning is  $\Delta\beta = 0$ , therefore the expression for the reflectivity becomes

$$R(l, \lambda) = \tanh^2(kl) \dots (5)$$

The reflectivity increases as the induced index of refraction change gets larger. Similarly, as the length of the grating increases, so does the resultant reflectivity.

### 3. Structural Health Monitoring

A typical health monitoring system is composed of a network of sensors that measure the parameters relevant to the state of the structure and its environment [2]. Nowadays structural health monitoring is a fundamental tool to assess the behaviour of existing structures but also to control the performance of large new structures, foreseen to give information to monitor their lifetime. In this paper, the monitoring of strain with optical fibre bragg grating sensors recorded in standard single mode optical fibers. Since FBG sensors are an all-in-fibre technology, they take advantage of the optical fibre properties, presenting also advantages over traditional electronic sensors due to the possibility to multiplex a large number of different sensors (temperature, displacement, pressure, pH value, humidity, high magnetic field and acceleration) into the same optical fibre, reducing the need for multiple and heavy cabling used in traditional electronic sensing.

### 4. Grating MOD

R-Soft is an optical simulator in which one of the tools GratingMOD is used for design and simulation of grating [3]. Any type of waveguide structure that can be defined in the R-Soft CAD interface can be treated as perturbed or, unperturbed waveguide in GratingMOD. Perturbation can be applied to index, width, height and both in combination. GratingMOD can simulate multiple types of grating profile and also can include multiple apodization types. Analysis and Synthesis are the two tools for simulation which facilitate to complete information of light wave field inside core of the fiber with gratings. Analysis simulation gives the information of reflectivity and transmittivity, modes, B.W.

- GratingMOD derived *via* couple mode theory based on orthogonal modes.
- Report has been compiled to understand the CAD Tool for Fiber Bragg Grating Sensor.
- MATLAB Simulation.

### 5. Simulation

The FBG sensors were designed with core diameter 8  $\mu\text{m}$  with refractive index of 1.47, and cladding diameter 125  $\mu\text{m}$  with refractive index 1.44. The gratings were inscribed over a length of about 3000  $\mu\text{m}$ . The magnitude of the photo-induced periodic modulation of refractive index

inside the core is generally of the order of  $10^{-5} - 10^{-2}$ . The grating periodicity produced with this phase mask was approximately  $\Lambda=0.5365\mu\text{m}$  and  $N_{\text{eff}}=1.464926$  giving a baseline Bragg wavelength around 1.57174 nm.

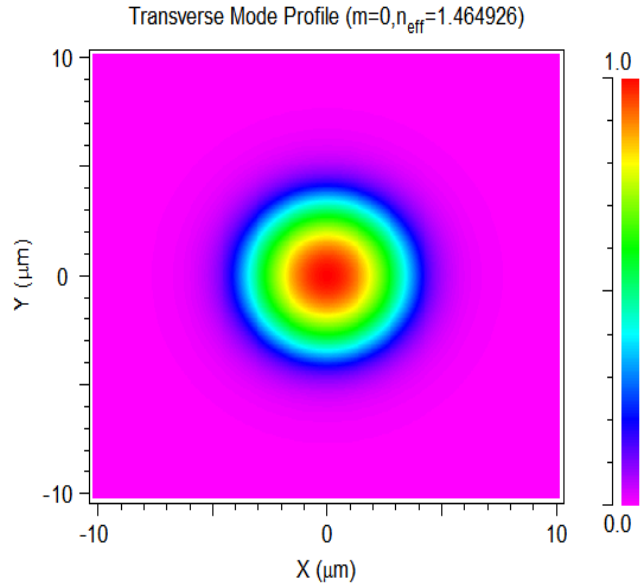


Fig 1. Computed modes for the Bragg grating

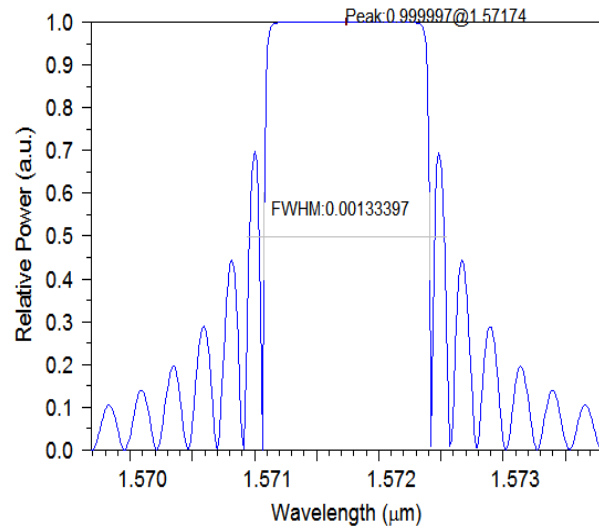


Fig 2. Computed reflection spectra Bragg wavelength at 1.57174  $\mu\text{m}$

Reflectivity increases as Grating length increases. For short period grating, concluded in paper [2], that for sensor application the reflectivity should be narrow spectral width.

The effect of elongating the optical fibre and thus the grating pitch has been simulated by taking the output graphs by varying the grating pitch from 0.5365  $\mu\text{m}$  to 0.540  $\mu\text{m}$  in regular intervals of 0.00035  $\mu\text{m}$ . Simulation

results in the form of graphs of reflected power as a function of wavelength. From iterations it has been established that at a grating pitch of  $0.5365\mu\text{m}$ , maximum reflected power is recorded at wavelength of  $1.550\mu\text{m}$ .

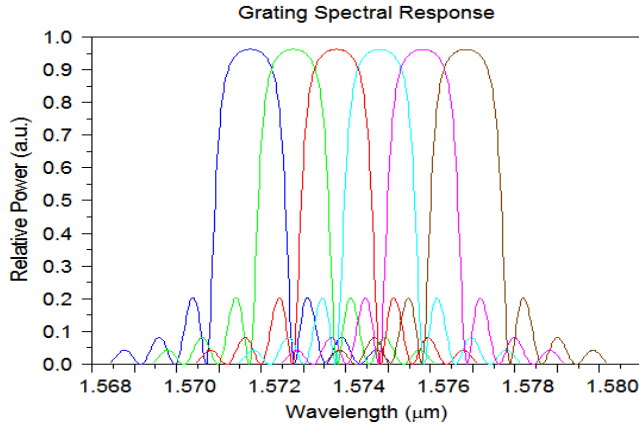


Fig 3. Grating periodicity produced with this phase mask was approximately  $\Lambda=0.5365\mu\text{m}$

### 5.1 Strain Sensitivity

The core effective index of refraction and the periodicity of the grating determine its center wavelength so that the change of fiber with strain will affect its core refractive index. The shift in the bragg grating center wavelength due to strain changes is given by [4]

$$\Delta\lambda_B = 2 \left( \Lambda \frac{dn_{eff}}{dL} + n_{eff} \frac{d\Lambda}{dL} \right) \Delta L \dots (6)$$

where T is temperature. The first term in equation (6) represents the strain effect on an optical fiber. The change in grating length, which is caused by a strain on the fiber will also affect the period of grating and the strain-optic induced refractive index.

The strain effect term could also be expressed by

$$\Delta\lambda_{B(s)} = \lambda_B (1 - p_e) \epsilon_z \dots (7)$$

Where  $\epsilon_z$  is the applied strain on the fiber grating longitudinal axis and  $p_e$  is an effective strain optic constant defined by

$$p_e = \frac{n_{eff}}{2} [p_{11} - \nu(p_{11} + p_{12})] \dots (8)$$

Where  $P_{11}$  and  $P_{12}$  are components of the strain-optic tensor,  $n_{eff}$  is the index of the core,  $\nu$  is Poisson's ratio. For a typical optical fiber and  $p_{11} = 0.113$ ,  $p_{12} = 0.252$ ,  $\nu =$

$0.16$  and  $n_{eff} = 1.482$ . By using these parameters and the above equations, the sensitivity of the Fiber Bragg Grating at  $1550\text{ nm}$  is about  $1.2\text{ pm}$  of the wavelength shift for  $1\mu\epsilon$  applied to the grating. Figure 4.1 shows the experimental results of wavelength dependence on applied strain for a  $1550.08\text{ nm}$  Fiber Bragg Grating.

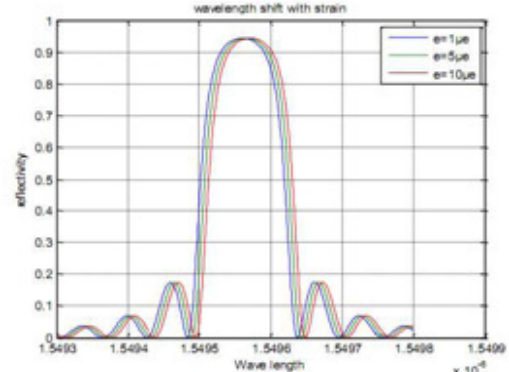


Fig 4. Spectrum Showing Wavelength Shift With Strain

### Strain Sensing code for analyzing the change in Strain for the applied pressure.

Axial Strain along FBG due to applied pressure 'P' is given by,

$$\epsilon - \text{Strain, } P - \text{Pressure, } \nu - \text{Poisson Ratio, } E - \text{Young's Modulus} \quad \epsilon = - \frac{P(1 - 2\nu)}{E} \dots (9)$$

CLC;

CLOSE ALL;

CLEAR ALL;

Pressure=0e6:0.5e6:100e6; %RANGE OF PRESSURE

VALUES IN MPA

$\nu=0.37$ ; %POISSON RATIO

$E=2.2e9$ ; %YOUNG'S MODULUS

Eps=-[Pressure\*(1-2\* $\nu$ )/E]; %PRESSURE SENSING EQUATION

plot(Pressure, Eps),grid; %PLOTING FUNCTION

title('Pressure Vs Strain');

xlabel('Pressure (MPa)');

ylabel(' Strain ( $\mu\text{m}$ )');

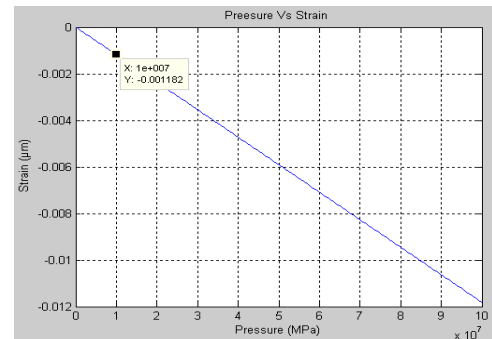


Fig 5. Depicts the Change in Strain with Change Pressure

### Strain Sensing code for equation (7) with certain assumed value for different parameters.

```
CLC;
CLEAR ALL;
CLEAR ALL;
Eps=[0:0.5:100]; %RANGE OF STRAIN VALUES
Pe=0.22;Lambda=1.55e-6; %BRAGGS CENTER WAVELENGTH
WavelengthShift=Lambda*(1-Pe).*Eps; %EQUATION FOR WAVELENGTH
plot(WavelengthShift, Eps),grid %PLOTING FUNCTION
title('Wavelength Shift Vs Strain ');
xlabel('Wavelength Shift (μm)');
ylabel(' Strain (μm)');
```

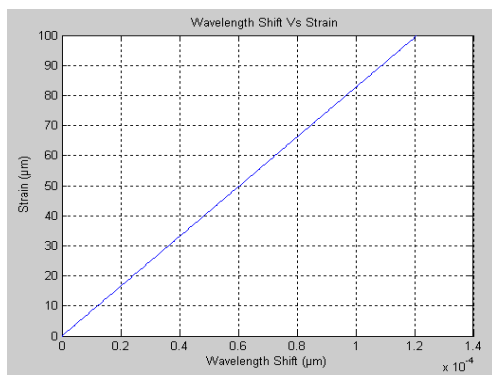


Fig 6. Depicts the change in wavelength with change in strain

### Strain Sensing code for equation (8) with certain assumed value for different parameters.

```
CLC;
CLOSE ALL;
CLEAR ALL;
P11= 0.113; %COMPONENTS OF STRAIN OPTIC TENSOR
P12= 0.252; %COMPONENTS OF STRAIN OPTIC TENSOR
NEFF=1.482; %EFFECTIVE REFRACTIVE INDEX
V=0.33; %POISSON RATIO
PE= (((NEFF ^2)/2)*(P12-V*(P11+P12))); %STRAIN OPTIC CONSTANT
LAMBDA=1550*10^-9; %BRAGGS CENTER WAVELENGTH
E= [0.000068, 0.000171, 0.0003166, 0.0005283]; %STRAIN VALUES
P= [0.012, 0.021, 0.05, 0.054]; %PRESSURE VALUES IN MPA
DELTALAMBDA=LAMBDA*(1-PE)*E;
%PRESSURE SENSING EQUATION
PLOT (P, DELTALAMBDA); %PLOTING FUNCTION
```

```
GRID;
XLABEL ('PRESSURE IN MPA');
YLABEL ('SHIFT IN WAVELENGTH ');
```

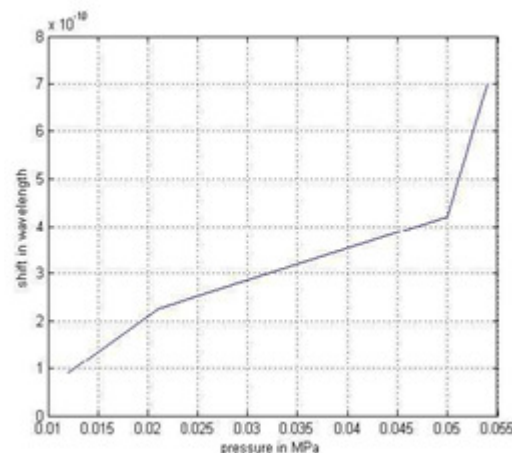


Fig 7. Depicts the Change in Wavelength with Change Pressure

## 6. Conclusion

Simulation results show the design parameter at  $L=1500\mu\text{m}$ , reflectivity 97.26% and FWHM  $=1.04\text{nm}$  for optical sensor by using mod-grating toolbox to achieve narrow spectral response which is very much required for high sensitivity. The modelled simulated parameters implemented for Strain sensor in the range of 1-10 $\mu\text{e}$  for structural health monitoring.

## References

- [1] Kashyap, R.: Fiber Bragg Gratings, San Diego, Academic Press, 1999, ISBN 0-12-400560-8
- [2] T.H.T. Chan, L. Yu, H.Y. Tam, Y.Q. Ni, S.Y. Liu, W.H. Chung and L.K. Cheng, "Fiber Bragg Grating sensors for structural health monitoring of Tsing Ma bridge: Background and experimental observation", Engineering Structures, vol. 28, Issue 5, pp. 648-659, April 2006.
- [3] [optics.synopsis.com/RSoft/GratingMOD](http://optics.synopsis.com/RSoft/GratingMOD)
- [4] T.H.T. Chan, L. Yu, H.Y. Tam, Y.Q. Ni, S.Y. Liu, W.H. Chung and L.K. Cheng, "Fiber Bragg Grating sensors for structural health monitoring of Tsing Ma bridge: Background and experimental observation", Engineering Structures, vol. 28, Issue5, pp. 648-659, April 2006.

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